Student's Name:

Lab day \& time: $\qquad$

Student's Name:
$\qquad$
Date: $\qquad$

## Archimedes' Principle (M8) - Data Sheets

(Show all calculations and write all results on the data sheets in ink)
Activity 1: Density
Diameter of the aluminum cylinder $\qquad$ ( )

Radius $r$ of the cylinder: $\quad r=$
Height of the cylinder: $\quad h=$ $\qquad$ ( )

Volume of the cylinder $\left(V_{l}\right)$ :

$$
V_{1}=
$$

Mass of the cylinder $\mathrm{m}_{1}$ (measured in air) $\qquad$ ( )

Weight of the cylinder ( W where $\mathrm{W}=\mathrm{m}_{1} \mathrm{~g}$ and $\mathrm{g}=9.80 \mathrm{~m} / \mathrm{s}^{2}$ ):

$$
W=
$$

Density of the aluminum cylinder:

Density $\rho_{\text {aluminum } 1}=$ $\qquad$ ( )

Calculate the absolute value of the percent difference between your result and the accepted value of the density of aluminum ( $2700 \mathrm{~kg} / \mathrm{m}^{3}$ ):

$$
\text { Percent difference }=\left|\frac{2700-\rho_{\text {aluminum } 1}}{2700}\right| * 100 \%=
$$

$\qquad$ (\%)

## Activity 2: Archimedes' Principle

For the weight $W$ of the aluminum cylinder in air use (copy) the value from Activity 1. $W=$ $\qquad$ ( )

Record the reading of the scale $\left(m_{2}\right)$ with the aluminum cylinder completely submerged in water.

$$
m_{2}=
$$

Apparent weight of the cylinder $\left(\mathrm{W}^{*}\right.$, where $\mathrm{W}^{*}=\mathrm{m}_{2} \mathrm{~g}$ and $\left.\mathrm{g}=9.80 \mathrm{~m} / \mathrm{s}^{2}\right)$ :

$$
W^{*}=
$$

Calculate density of the aluminum cylinder based on the Archimedes' principle. Remember that the density of water is equal to: $\rho_{w}=1000 \mathrm{~kg} / \mathrm{m}^{3}$.

$$
\rho_{\text {aluminum } 2}=\frac{W}{\left(W-W^{*}\right)} \rho_{w}
$$

Density $\rho_{\text {aluminum } 2}=$ $\qquad$ (

Calculate the absolute value of the percent difference between your result and the accepted value of the density of aluminum $\left(2700 \mathrm{~kg} / \mathrm{m}^{3}\right)$ :

$$
\text { Percent difference }=\left|\frac{2700-\rho_{\text {aluminum } 2}}{2700}\right| * 100 \%=
$$

$\qquad$ (\%)

Calculate the absolute value of the percent difference between the two measurements
(Activity 1 and Activity 2) of density of aluminum.

$$
\text { Percent difference }=\left|\frac{\rho_{\text {aluminum } 1}-\rho_{\text {aluminum } 2}}{\rho_{\text {alumimum } 2}}\right| \times 100 \%=
$$

$\qquad$ (\%)

Do we need a correction for the density of air?
Strictly speaking, when we measure mass of the aluminum cylinder in air, we should also consider the buoyant force due to the air. Let us make an estimate to see how big is that correction. Consider an aluminum cylinder that has mass $\mathrm{m}=0.10 \mathrm{~kg}$ (close to the mass of
the cylinder that we are using in this experiment). The density of aluminum is $2700 \mathrm{~kg} / \mathrm{m}^{3}$ and the density of air at room temperature $20^{\circ} \mathrm{C}$ is equal to $\rho_{\text {air }}=1.21 \mathrm{~kg} / \mathrm{m}^{3}$.

The volume of the cylinder $\mathrm{V}=\mathrm{m} / \rho_{\text {aluminum }}=0.10 \mathrm{~kg} / 2700 \mathrm{~kg} / \mathrm{m}^{3}=3.7 * 10^{-5} \mathrm{~m}^{3}$
The buoyant force due to the air displaced by the cylinder is equal to:

$$
\mathrm{F}_{\mathrm{b} \text { air }}=\rho_{\text {air }} \mathrm{Vg}=1.21 \mathrm{~kg} / \mathrm{m}^{3} * 3.7 * 10^{-5} \mathrm{~m}^{3} * 9.8 \mathrm{~m} / \mathrm{s}^{2}=4.4^{*} 10^{-4} \mathrm{~N}
$$

The error that we made during the mass measurement because we neglected buoyant force due to displaced air is equal to $\mathrm{F}_{\mathrm{b} \text { air }} / \mathrm{g}=\rho_{\text {air }} \mathrm{V}=4.5^{*} 10^{-5} \mathrm{~kg}=0.045 \mathrm{~g}$. You cannot measure mass with this accuracy using the available scale. Therefore, the correction is small enough to be ignored.

## Activity 3: Density of Glass

In this activity, measure the density of irregularly shaped glass stopper.

Measured mass (in air) $\mathrm{m}_{\text {glass } 1}=$ $\qquad$ ( )

Calculate the weight of the Pyrex glass object in air (W, where $\left.W=\mathrm{m}_{\text {glass } 1} \mathrm{~g}\right)$ :

$$
W=\longrightarrow(\quad)
$$

Record the reading of the scale ( $\mathrm{m}_{\text {glass } 2}$ ) with the glass object completely submerged in water.

$$
\mathrm{m}_{\text {glass } 2}=
$$

Apparent weight of the glass object in water $\left(\mathrm{W}^{*}\right.$, where $\left.\mathrm{W}^{*}=\mathrm{m}_{\text {glass } 2} \mathrm{~g}\right)$ :

$$
W^{*}=
$$

Volume of the glass piece (use Eq. (2)):

$$
V_{\text {glass }}=\square(\quad)
$$

Calculate density of the Pyrex glass piece based on the Archimedes' principle. Remember that the density of water is equal to: $\rho_{w}=1000 \mathrm{~kg} / \mathrm{m}^{3}$.
$\rho_{\text {glass }}=\frac{W}{\left(W-W^{*}\right)} \rho_{w}$

Density $\rho_{g \text { gass }}=$ $\qquad$ ( )

Calculate the absolute value of the percent difference between your result and the accepted value of the density of aluminum ( $2230 \mathrm{~kg} / \mathrm{m}^{3}$ ):

$$
\text { Percent difference }=\left|\frac{2230-\rho_{\text {glass }}}{2230}\right| * 100 \%=
$$

$\qquad$ (\%)

## Activity 4: Two-Metal Cylinder

The two-metal cylinder is made with a mix of aluminum and brass. There are no empty cavities inside the mixed cylinder. Your goal is to find what is the composition of this cylinder, i.e., what is the percentage of brass and aluminum.

Measured mass:
$m$ (in air) $\qquad$ ( )

Weight of the brass/aluminum cylinder in air:

$$
W=\ldots(\quad)
$$

Record the reading of the scale $\left(m_{2}\right)$ with the brass/aluminum cylinder completely submerged in water.

$$
m_{2}=
$$

Apparent weight of the brass/aluminum cylinder in water $\left(\mathrm{W}^{*}=\mathrm{m}_{2} \mathrm{~g}\right)$ :

$$
W^{*}=\ldots(\quad)
$$

Calculate the volume of the cylinder. (Hint: use Eq. (2) from M8 - Theory and Procedures file).

$$
V=
$$

$\qquad$ ( )

Calculate the volume of the brass in the two-metal cylinder $\left(\mathrm{V}_{\text {brass }}\right)$ using the provided density of brass $\left(\rho_{1}=8600 \mathrm{~kg} / \mathrm{m}^{3}\right)$ and density of aluminum $\left(\rho_{2}=2700 \mathrm{~kg} / \mathrm{m}^{3}\right)$.

$$
V_{\text {brass }}=\mathrm{W}^{*}\left(\frac{\rho_{2}}{\rho_{w}\left(\rho_{1}-\rho_{2}\right) g}\right)-W\left(\frac{\rho_{2}-\rho_{w}}{\rho_{w}\left(\rho_{1}-\rho_{2}\right) g}\right)
$$

(where: $\rho_{\mathrm{W}}=1000 \mathrm{~kg} / \mathrm{m}^{3}, \rho_{1}=8600 \mathrm{~kg} / \mathrm{m}^{3}$ and $\rho_{2}=2700 \mathrm{~kg} / \mathrm{m}^{3}$ )

$$
V_{\text {brass }}=\square(\quad)
$$

Percentage of the volume that is brass in the two-metal cylinder $\left(100 \% * \mathrm{~V}_{\text {brass }} / \mathrm{V}\right)$ :

Volume percentage of brass $=$ $\qquad$ (\%)

Volume of the aluminum in the cylinder $\left(\mathrm{V}_{\mathrm{Al}}=\mathrm{V}-\mathrm{V}_{\text {brass }}\right)$ :

$$
V_{A l}=
$$

Percentage of the volume that is aluminum in the two-metal cylinder $\left(100 \% * \mathrm{~V}_{\mathrm{Al}} / \mathrm{V}\right)$ :

Volume percentage of aluminum= $\qquad$ (\%)

Mass of the brass in the two-metal cylinder $\left(\rho_{1} V_{\text {brass }}\right.$, where $\left.\rho_{1}=8600 \mathrm{~kg} / \mathrm{m}^{3}\right)$ :

$$
\rho_{1} V_{\text {brass }}=
$$

Percentage of the brass mass in the two-metal cylinder $\left(100 \% * \rho_{1} \mathrm{~V}_{\text {brass }} / \mathrm{m}\right)$ :

$$
\text { Percentage }=
$$

$\qquad$ (\%)

Mass of the aluminum that is in the two $=$ metal cylinder $\left(\rho_{2} V_{\mathrm{Al}}\right.$, where: $\left.\rho_{2}=2700 \mathrm{~kg} / \mathrm{m}^{3}\right)$ : $\rho_{2} \mathrm{~V}_{\mathrm{Al}}=$ $\qquad$ ( )

Percentage of the mass that is aluminum $\left(100 \% 0^{*} \rho_{2} \mathrm{~V}_{\mathrm{Al}} / \mathrm{m}\right)$ :

Percentage $=$ $\qquad$ (\%)

This is the last activity. Dump the water into the lab sink and make sure that there is no water on the table. Wipe the table with paper towels if necessary. Thanks!

Complete the lab report and return it to the lab TA.

